Graphentheorie
3. Übungsblatt WS 05/06

Abgabetermin: 14.11.05

## Exercise 11

Prove that a graph is connected iff for every partition $V(G)=V_{1} \cup V_{2}$, there exists an edge of $G$ joining a vertex of $V_{1}$ and a vertex of $V_{2}$.

## Exercise 12

Let $G$ be a graph with $V(G)=\left\{v_{1}, v_{2}, \ldots, v_{7}\right\}$ such that $G-v_{i}=K_{2,4}$ for $i=1,2,3$ and $G-v_{i}=K_{3,3}$ for $i=4,5,6,7$. Show that $G$ is reconstructible.

## Exercise 13

Determine the labeled tree having Prüfer sequence (4, 5, 7, 2, 1, 1, $6,6,7)$.

## Exercise 14

Let $v$ be a fixed vertex of $G=K_{n}$. Determine the number of spanning trees of $G$ in which $v$ is an end-vertex.

## Exercise 15

Are there graphs $G$ of order $n$ other than $K_{n}$ with $a(G)=\left\lceil\frac{n}{2}\right\rceil$ ?

